

# Formal Methods for Wireless Mesh Networks

Peter Höfner

München

February 17, 2012



Australian Government

Department of Broadband, Communications  
and the Digital Economy

Australian Research Council

NICTA Members



Department of State and  
Regional Development



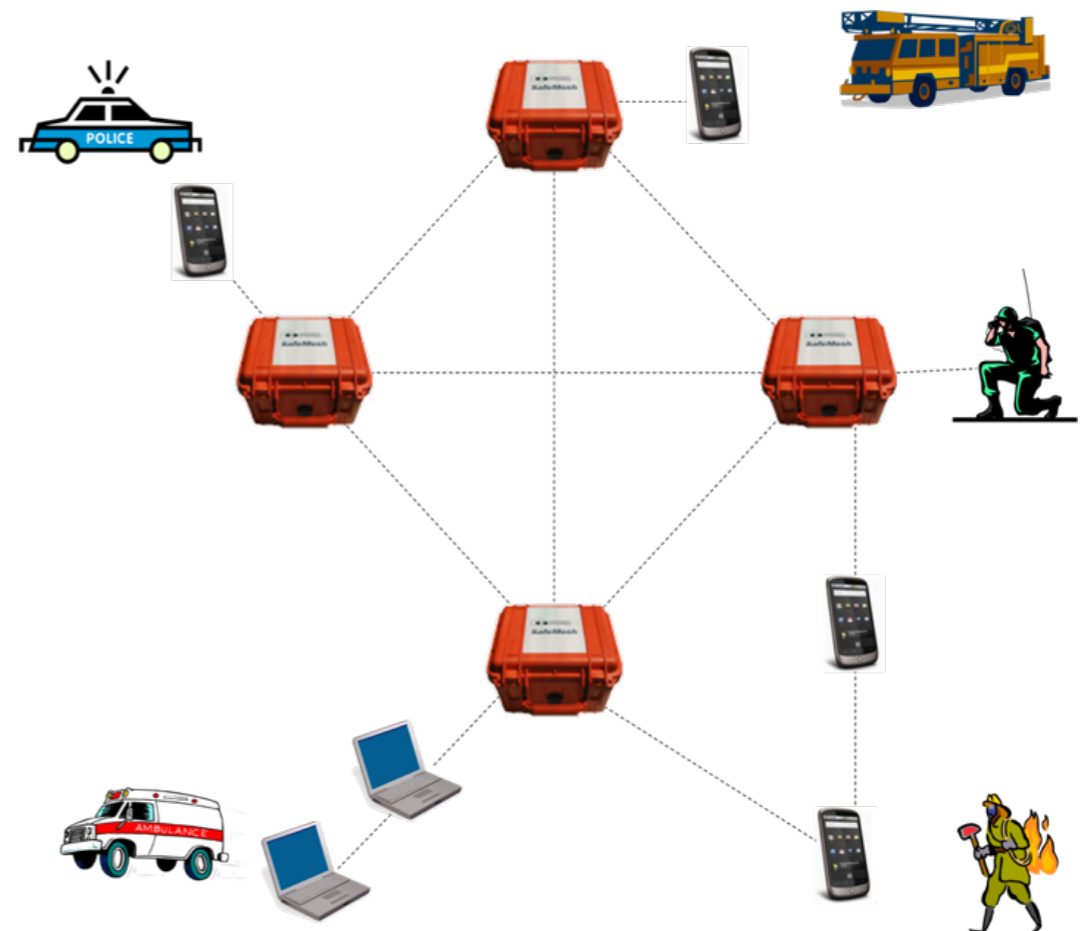
The University of Sydney



NICTA Partners

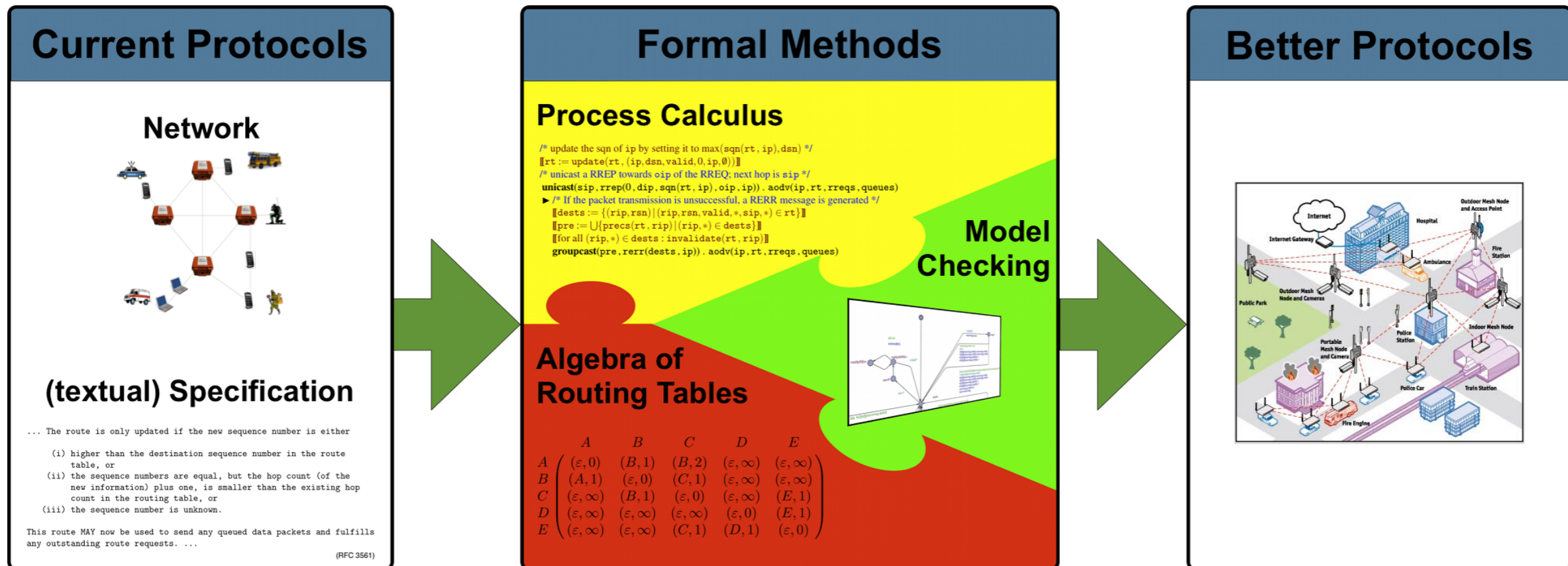
# What is the Problem?

- **Wireless Mesh Networks (WMNs)**
  - key features: mobility, dynamic topology, wireless multihop backhaul
  - quick and low cost deployment
- **Applications**
  - public safety
  - emergency response, disaster recovery
  - transportation
  - mining
  - smart grid
  - ...
- **Limitations in reliability and performance**



- **Goal**
  - model, analyse, verify and increase the performance of wireless mesh protocols
  - develop suitable formal methods techniques
- **Benefits**
  - more reliable protocols
  - finding and fixing bugs
  - better performance
  - proving correctness
  - reduce “time-to-market”
- **Team (Formal Methods)**
  - Ansgar Fehnker, Rob van Glabbeek, Peter Höfner, Annabelle McIver, Marius Portmann, Wee Lum Tan

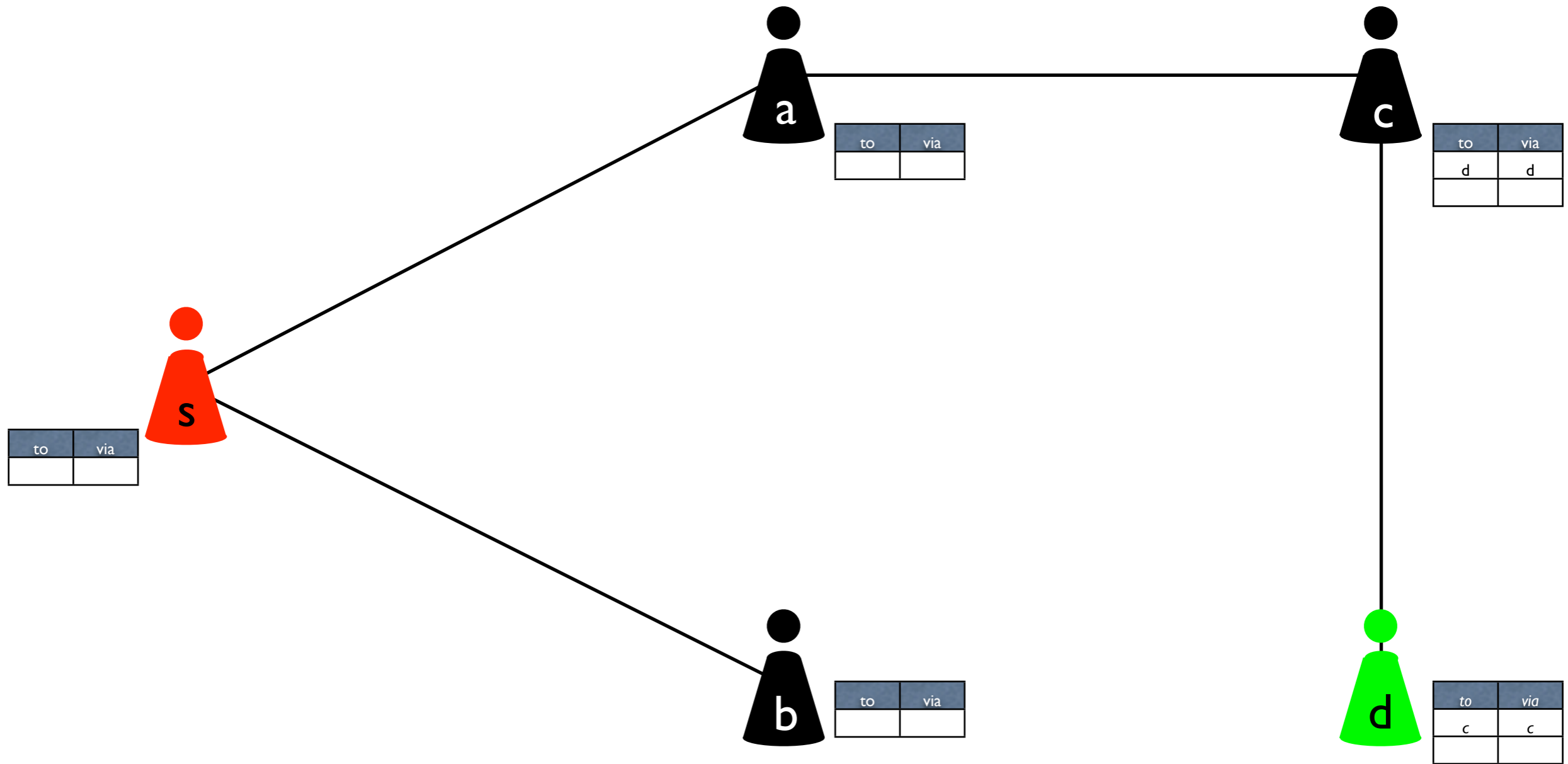
- Main Methods used so far
  - process algebra
  - model checking
  - routing algebra



- Routing protocol for WMNs
- Ad hoc (network is not static)
- On-Demand (routes are established when needed)
- Distance (metric is hop count)
- Vector (routing table has the form of a vector)
- Developed 1997-2001 by Perkins, Beldig-Royer and Das (University of Cincinnati)

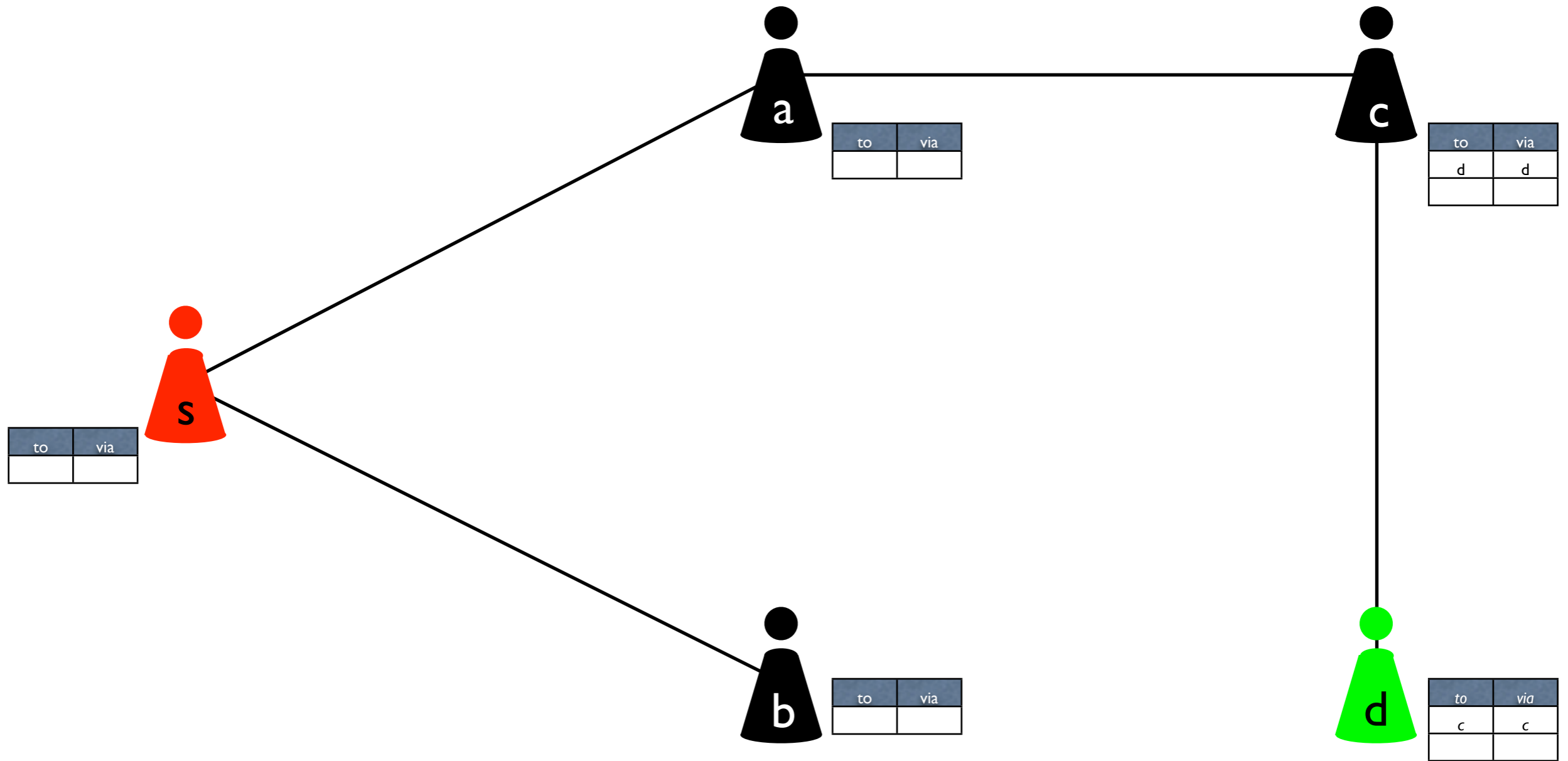
- AODV control messages
  - route request (RREQ)
  - route reply (RREP)
  - route error message (RERR)
  
- Main Mechanism
  - if route is needed  
BROADCAST RREQ
  - if node has information about a destination  
UNICAST RREP
  - if unicast fails or link break is detected  
SEND RERR

# AODV – An Example



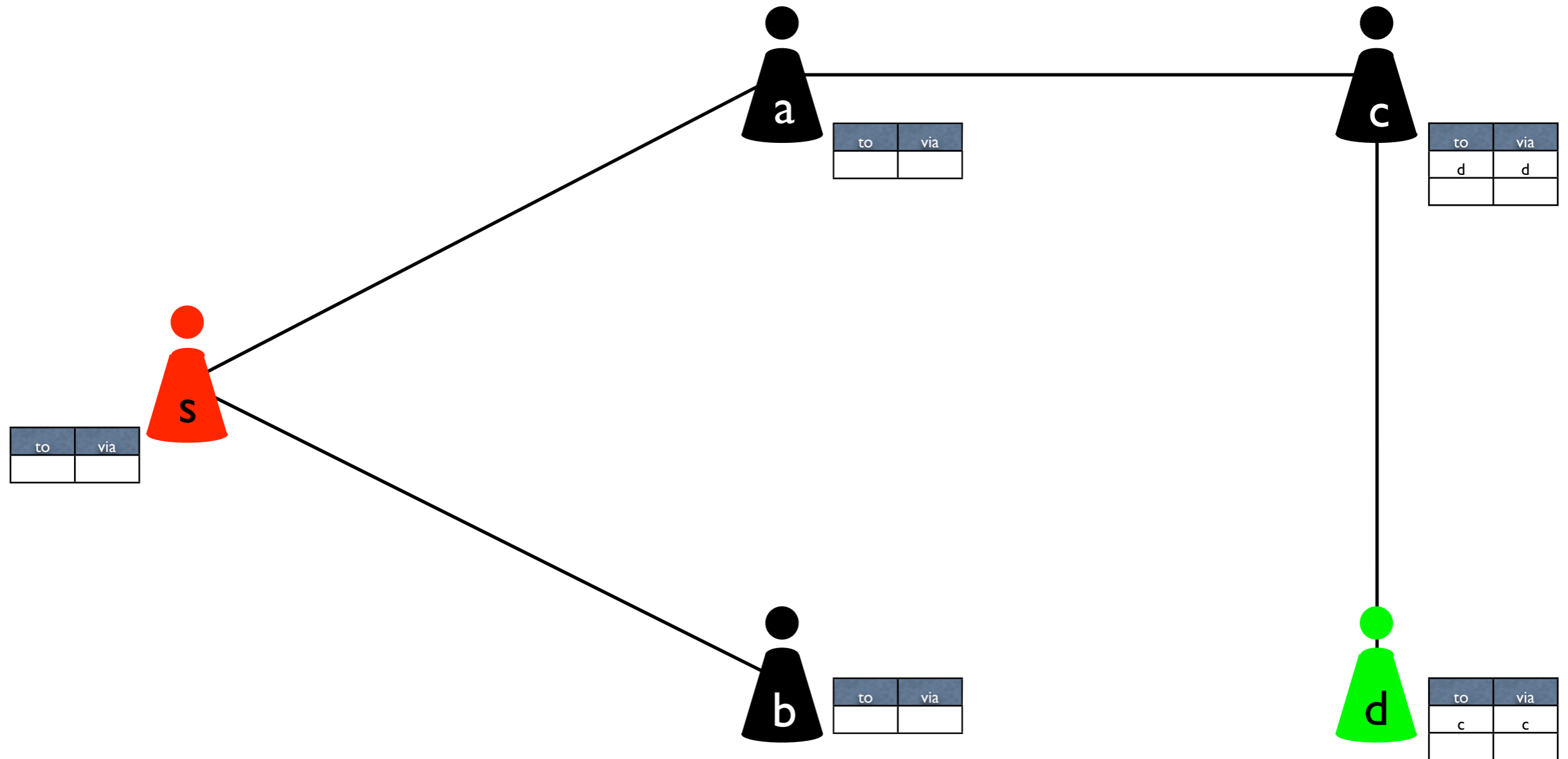
s is looking for a route to d

# AODV – An Example

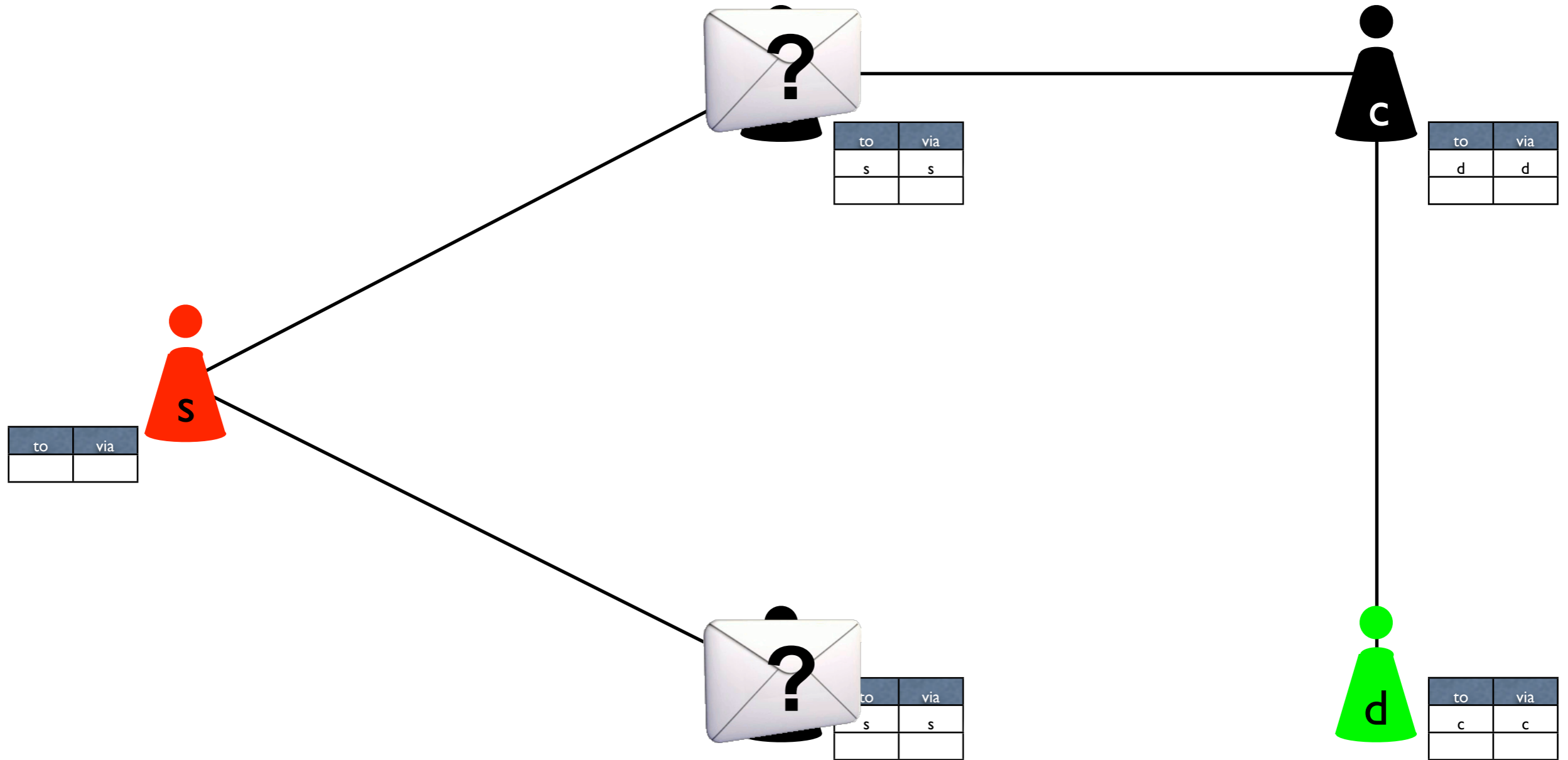




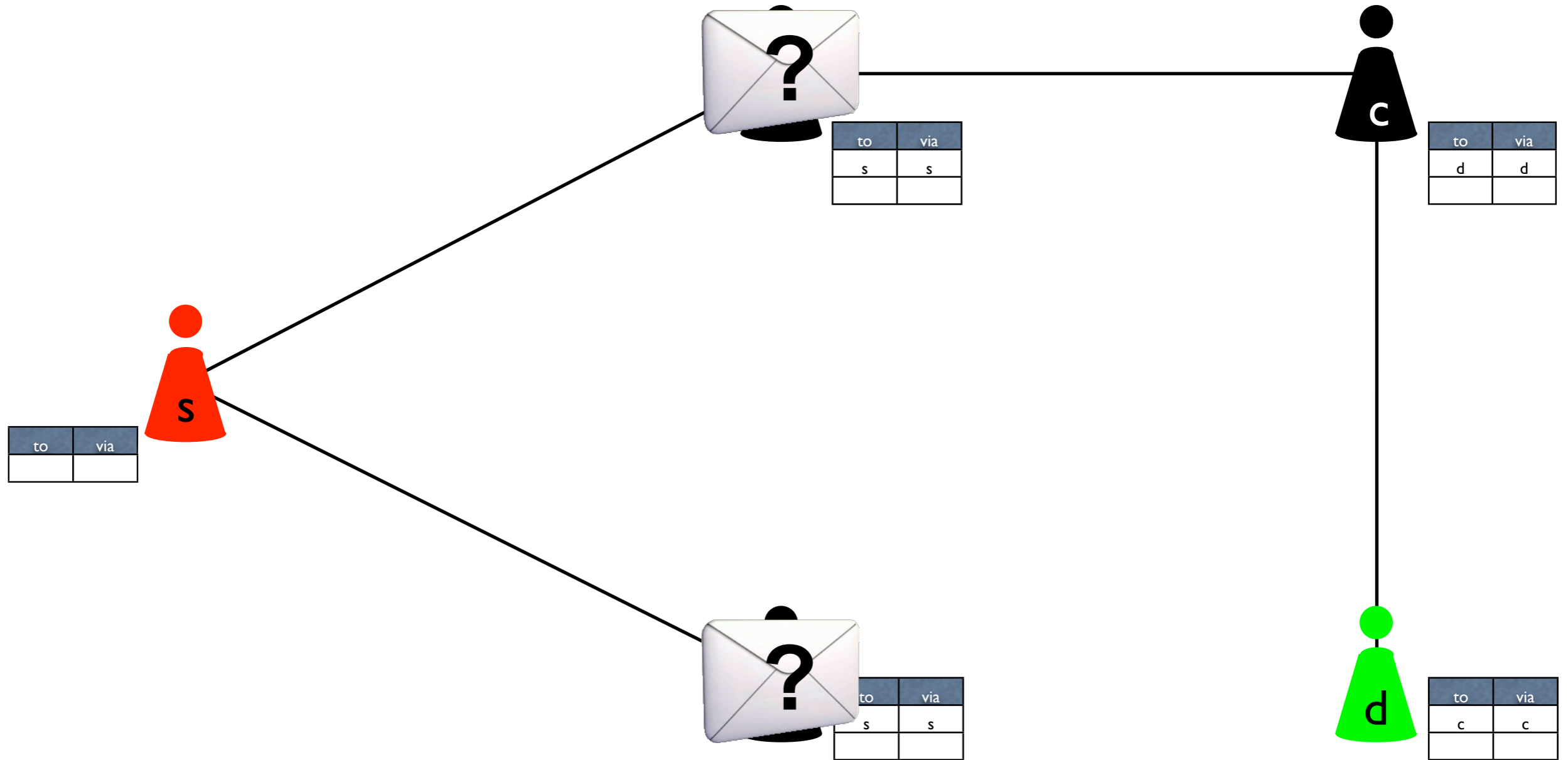
# AODV – An Example



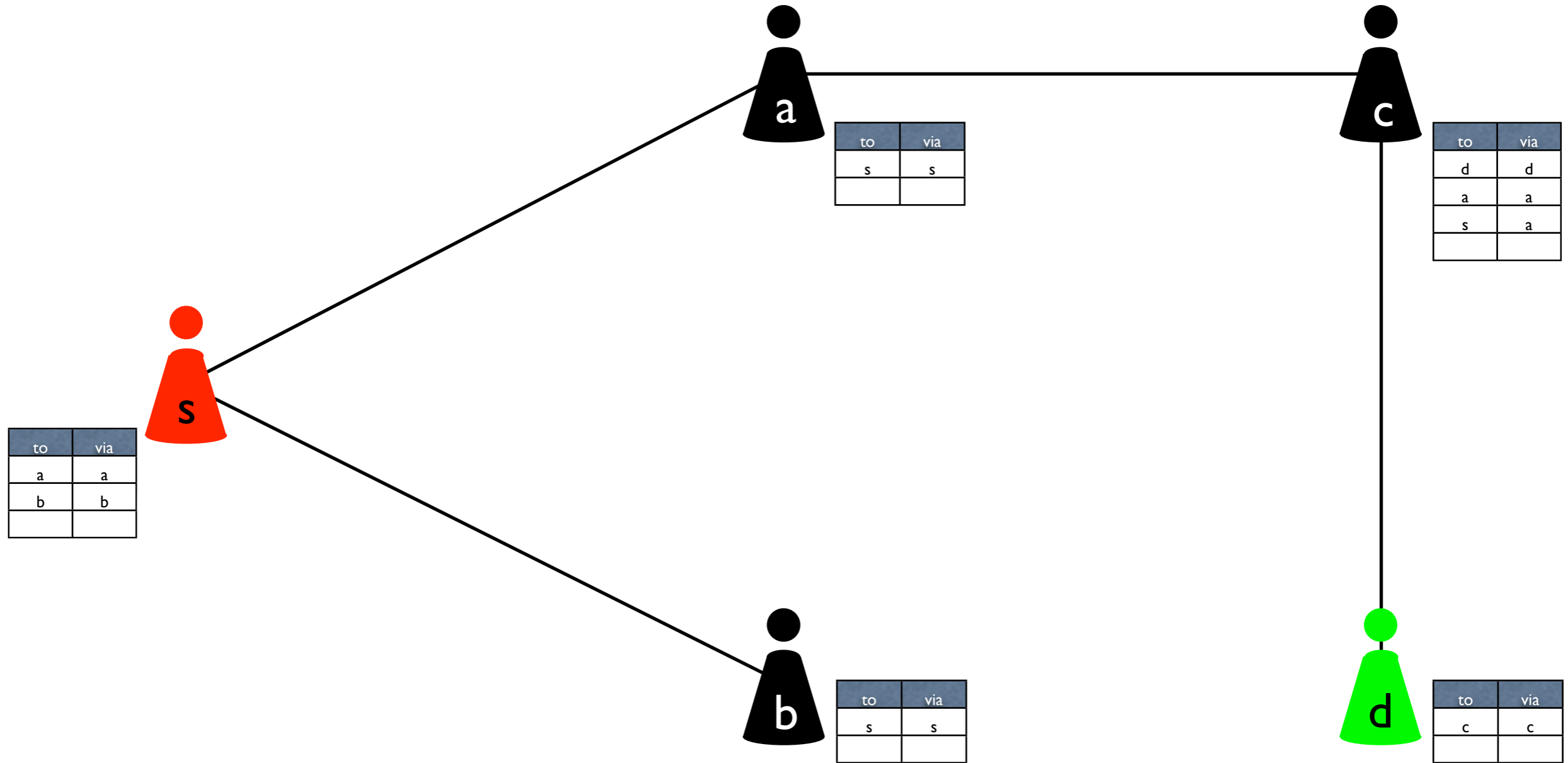
# AODV – An Example



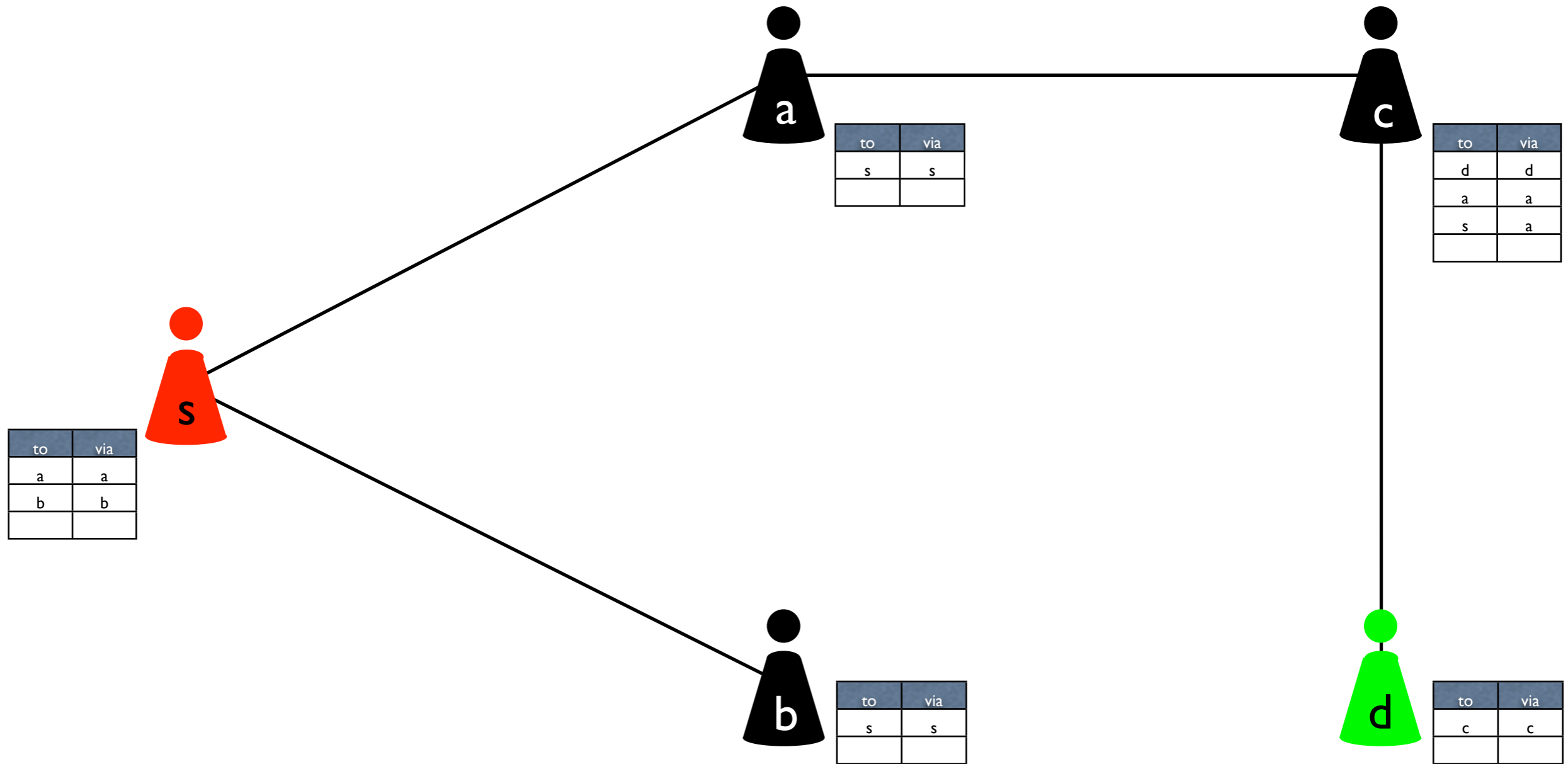
# AODV – An Example



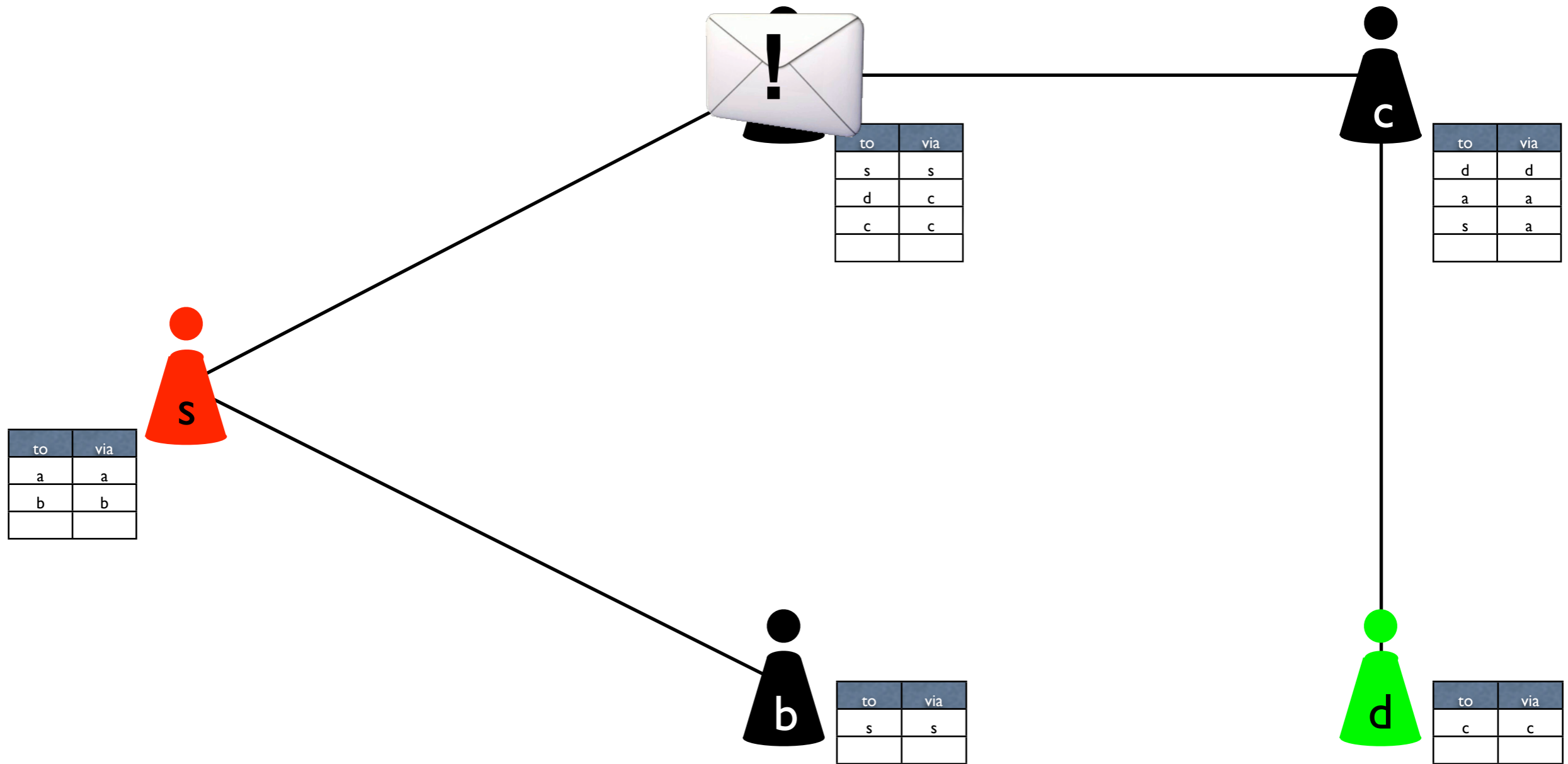
# AODV – An Example



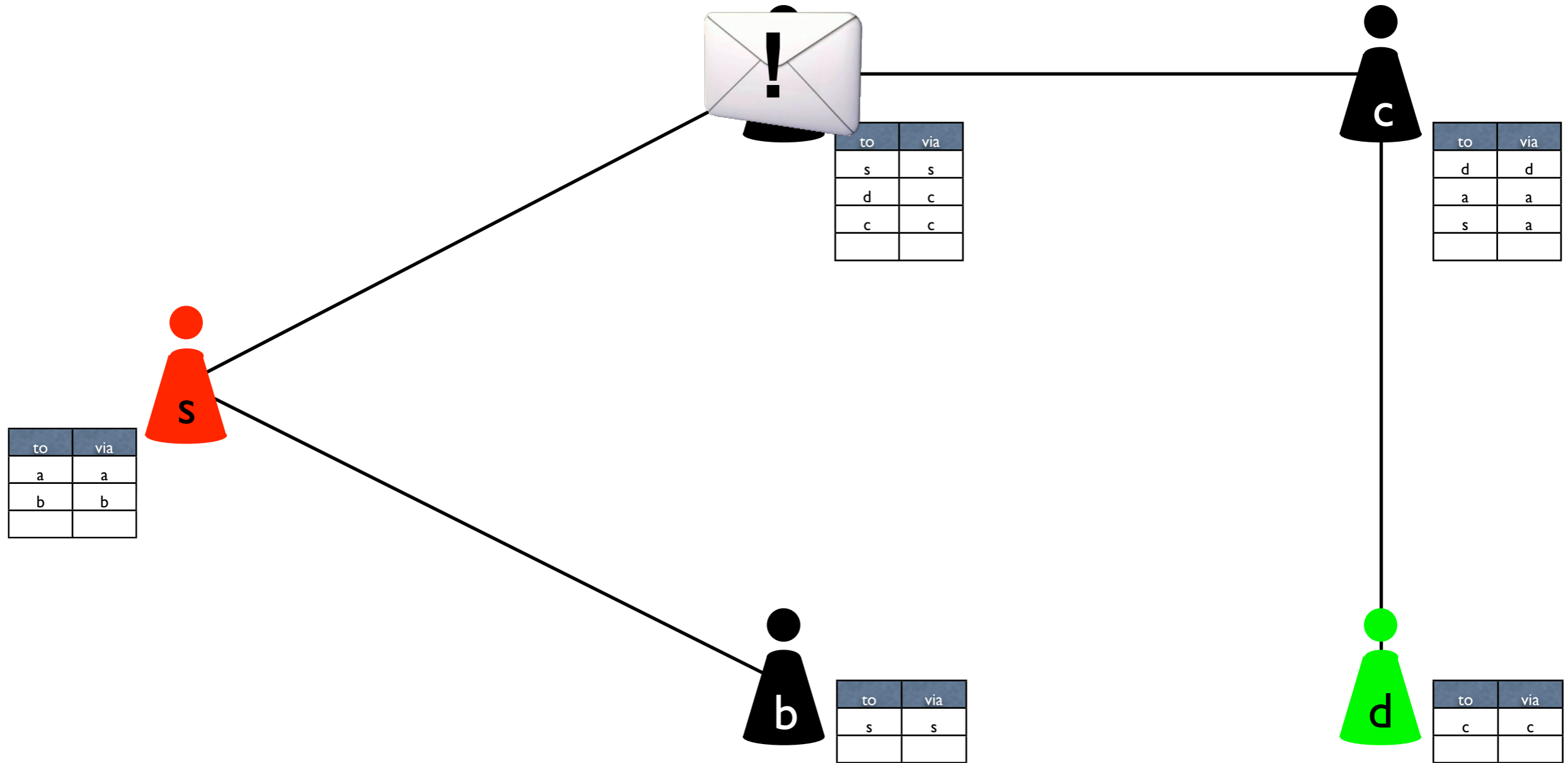
# AODV – An Example



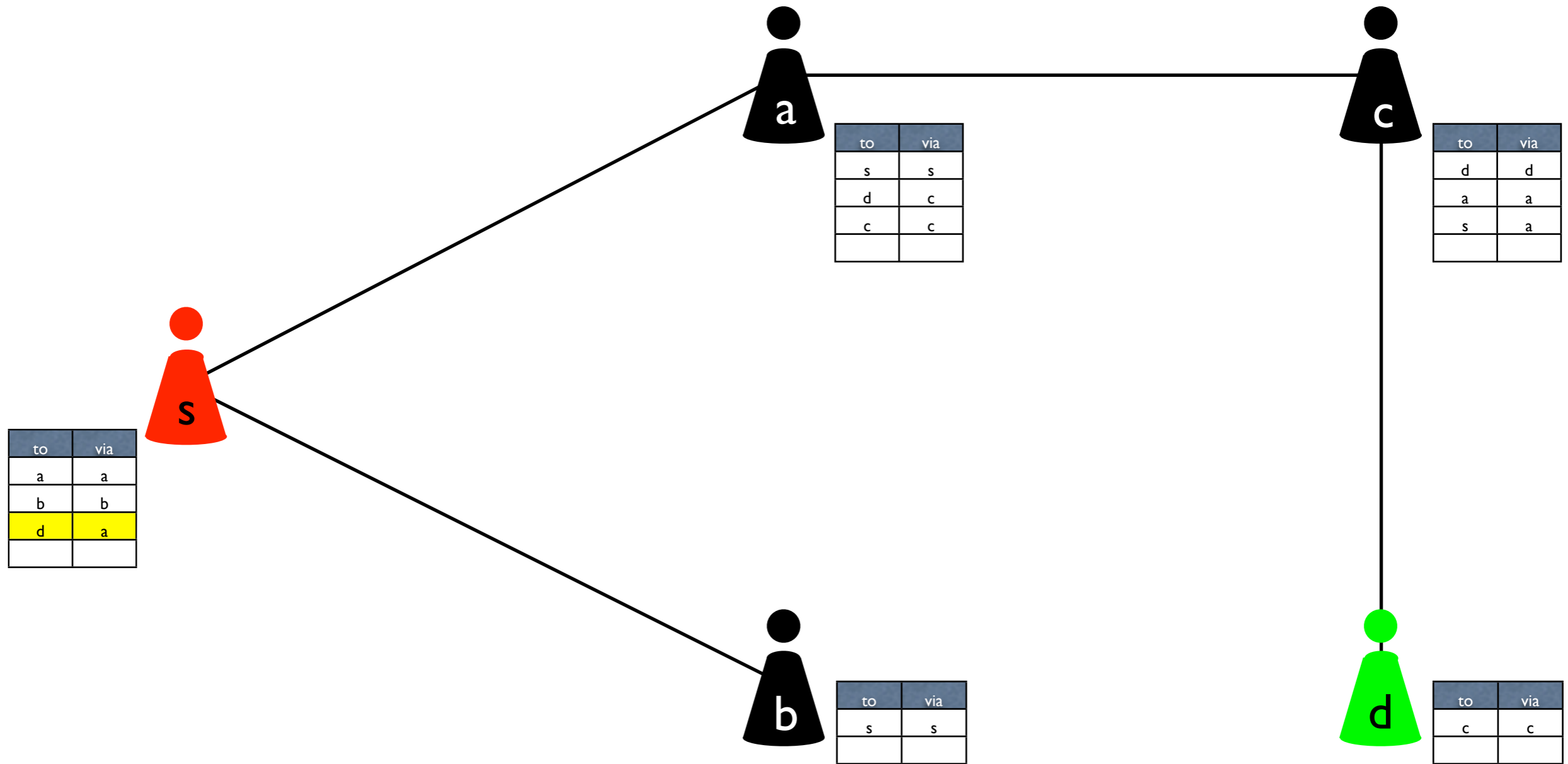
# AODV – An Example



# AODV – An Example

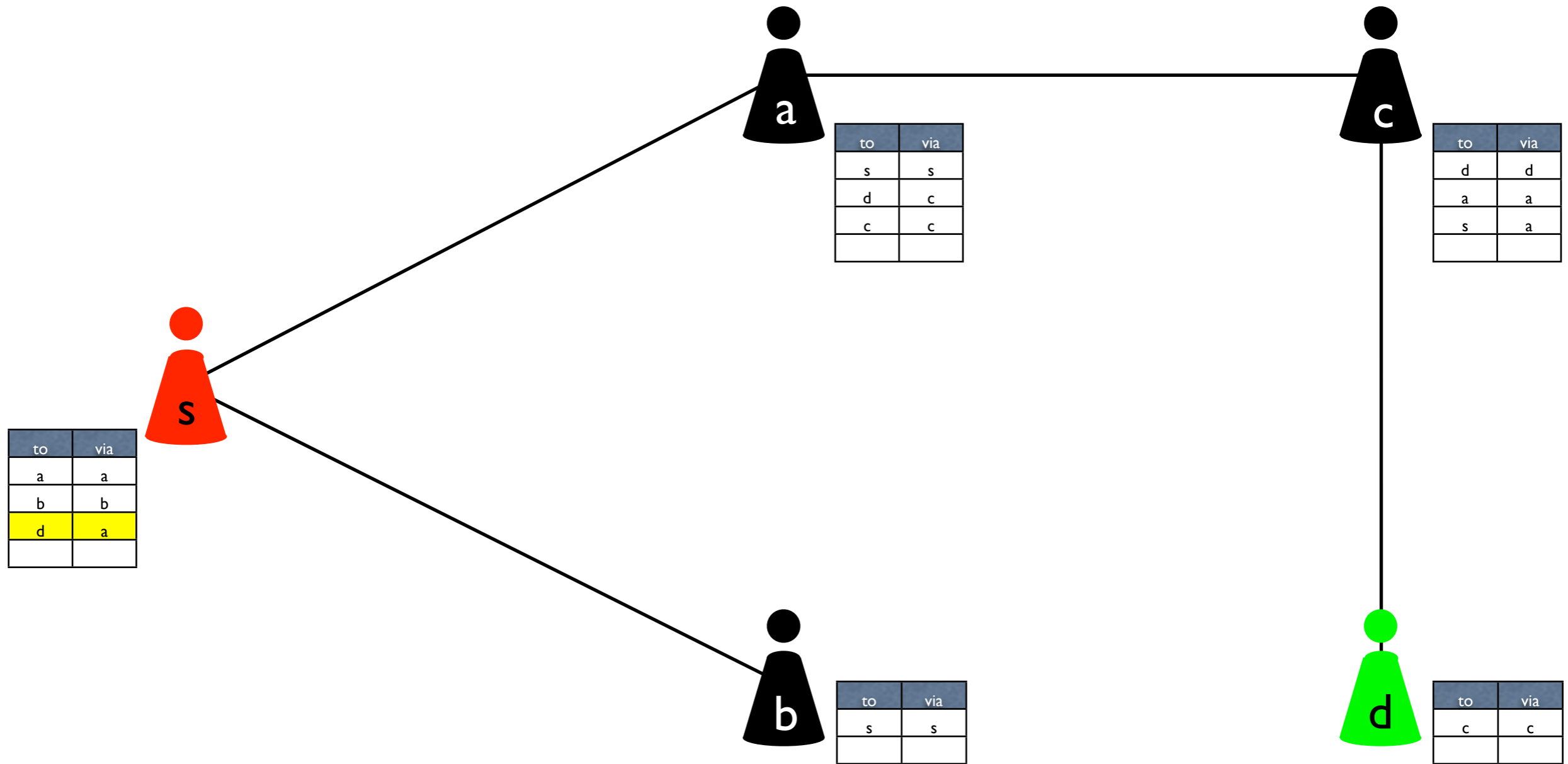


# AODV – An Example

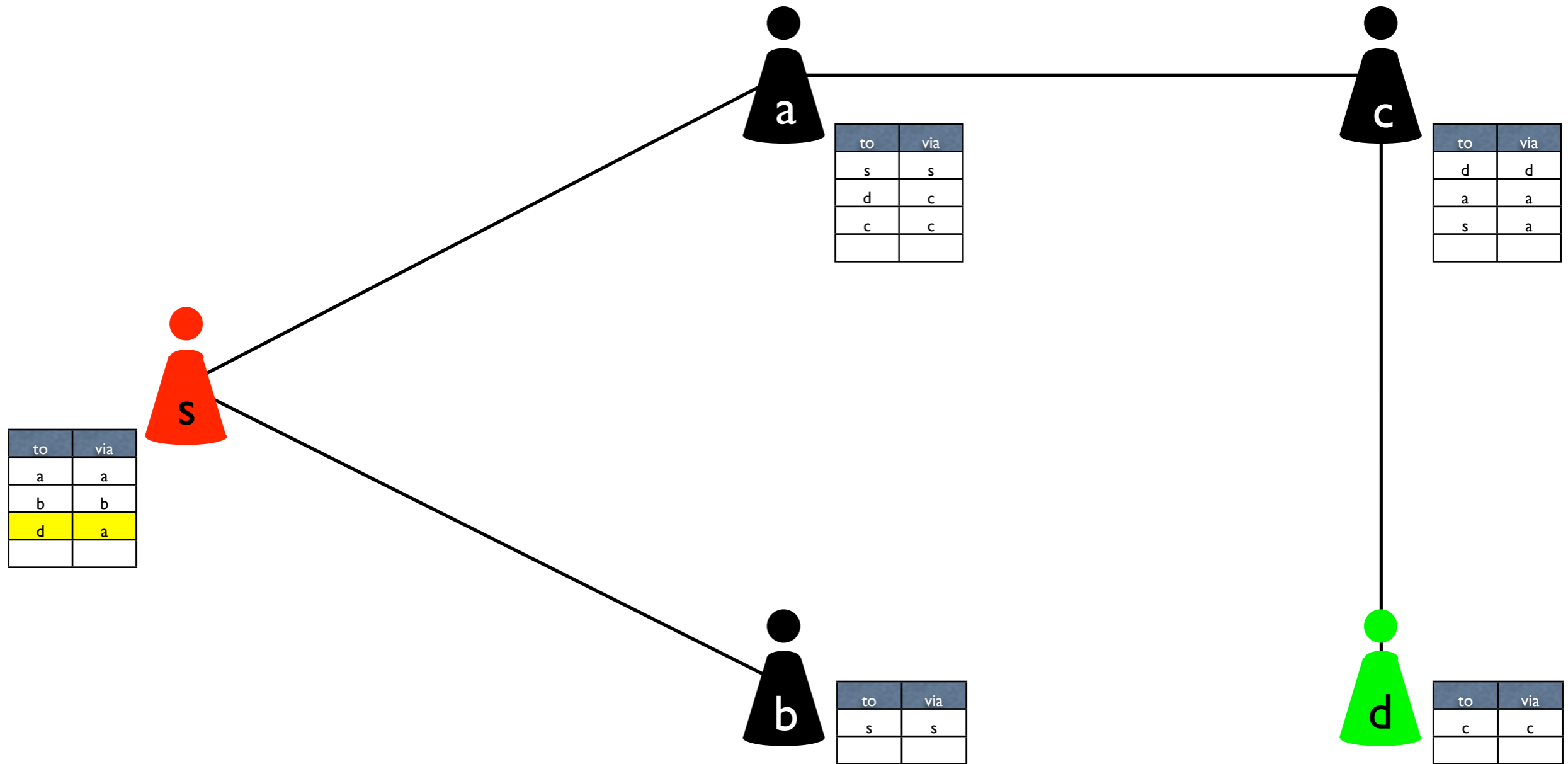




# AODV – An Example



# AODV – An Example



s has found a route to d

- Properties of AODV
  - route correctness
  - loop freedom
  - route discovery
  - packet delivery

- Properties of AODV

- route correctness



- loop freedom



(at least for some interpretations)

- route discovery



- packet delivery



- Properties of AODV

- route correctness



- loop freedom



- route discovery



- packet delivery



- so far only simulation and test-bed evaluations

- important, valid methods

- limitations

- resource intensive, time-consuming, no generality

- Properties of AODV

- route correctness



- loop freedom



(at least for some interpretations)

- route discovery



- packet delivery



- so far only simulation and test-bed evaluations

- important, valid methods

- limitations

- resource intensive, time-consuming, no generality

- Request for Comments (de facto standard)

sequence number field is set to false. The route is only updated if the new sequence number is either

- (i) higher than the destination sequence number in the route table, or
- (ii) the sequence numbers are equal, but the hop count (of the new information) plus one, is smaller than the existing hop count in the routing table, or
- (iii) the sequence number is unknown.

```
+ [ (oip, rreqid) ∉ rreqs ]      /* the RREQ is new to this node */
  /* update the route to oip in rt */
  [[rt := update(rt, (oip, osn, valid, hops + 1, sip, ∅))]]
  /* update rreqs by adding (oip, rreqid) */
  [[rreqs := rreqs ∪ {(oip, rreqid)}]]
  (
    [ dip = ip ]      /* this node is the destination node */
    /* update the sqn of ip by setting it to max(sqn(rt, ip), dsn) */
    [[rt := update(rt, (ip, dsn, valid, 0, ip, ∅))]]
    /* unicast a RREP towards oip of the RREQ; next hop is sip */
    unicast(sip, rrep(0, dip, sqn(rt, ip), oip, ip)). AODV(ip, rt, rreqs, queues)
    ► /* If the packet transmission is unsuccessful, a RERR message is generated */
    [[dests := {(rip, rsn) | (rip, rsn, valid, *, sip, *) ∈ rt}]]
    [[pre := ∪ {precs(rt, rip) | (rip, *) ∈ dests}]]
    [[for all (rip, *) ∈ dests : invalidate(rt, rip)]]
    groupcast(pre, rerr(dests, ip)). AODV(ip, rt, rreqs, queues)
  )
+ [ dip ≠ ip ]      /* this node is not the destination node */
  (
    [ dip ∈ aD(rt) ∧ dsn ≤ sqn(rt, dip) ∧ sqn(rt, dip) ≠ 0 ]      /* valid route to dip that is
    fresh enough */
    /* update rt by adding sip to precs(rt, dip) */
    [[r := addpre(σroute(rt, dip), {sip}); rt := update(rt, r)]]
  )
```



- **Desired Properties**
  - guaranteed broadcast
  - conditional unicast
  - data structure
  
- **Inspired by**
  - $\pi$ - Calculus
  - $\omega$ - Calculus
  - (LOTOS)

- User
  - Network as a “cloud”
- Collection of nodes
  - connect / disconnect / send / receive
  - “parallel execution” of nodes
- Nodes
  - data management
    - data packets, messages, IP addresses ...
  - message management (avoid blocking)
  - core management
    - broadcast / unicast / groupcast ...
  - “parallel execution” of sequential processes

- Syntax of sequential process expressions

$$SP ::= X(exp_1, \dots, exp_n) \mid [\varphi]SP \mid \llbracket \text{var} := exp \rrbracket SP \mid SP + SP \mid$$
$$\alpha.SP \mid \mathbf{unicast}(dest, ms).SP \blacktriangleright SP$$
$$\alpha ::= \mathbf{broadcast}(ms) \mid \mathbf{groupcast}(dests, ms) \mid \mathbf{send}(ms) \mid$$
$$\mathbf{deliver}(data) \mid \mathbf{receive}(msg)$$

- internal state determined by expression and valuation

$$\begin{array}{l} \xi, \mathbf{broadcast}(ms).p \xrightarrow{\mathbf{broadcast}(\xi(ms))} \xi, p \\ \xi, \mathbf{groupcast}(dests, ms).p \xrightarrow{\mathbf{groupcast}(\xi(dests), \xi(ms))} \xi, p \\ \xi, \mathbf{unicast}(dest, ms).p \blacktriangleright q \xrightarrow{\mathbf{unicast}(\xi(dest), \xi(ms))} \xi, p \\ \xi, \mathbf{unicast}(dest, ms).p \blacktriangleright q \xrightarrow{\neg \mathbf{unicast}(\xi(dest))} \xi, q \\ \xi, \mathbf{send}(ms).p \xrightarrow{\mathbf{send}(\xi(ms))} \xi, p \\ \xi, \mathbf{deliver}(data).p \xrightarrow{\mathbf{deliver}(\xi(data))} \xi, p \\ \xi, \mathbf{receive}(msg).p \xrightarrow{\mathbf{receive}(m)} \xi[msg := m], p \quad (\forall m \in \text{MSG}) \end{array}$$

- Node expressions:  $M ::= ip : P : R \mid M || M$
- Operational Semantics (snippet)

$$\frac{P \xrightarrow{\text{broadcast}(m)} P'}{ip : P : R \xrightarrow{R : * \text{cast}(m)} ip : P' : R}$$

$$\frac{P \xrightarrow{\text{unicast}(dip, m)} P' \quad dip \in R}{ip : P : R \xrightarrow{\{dip\} : * \text{cast}(m)} ip : P' : R} \quad \frac{P \xrightarrow{\neg \text{unicast}(dip)} P' \quad dip \notin R}{ip : P : R \xrightarrow{\tau} ip : P' : R}$$

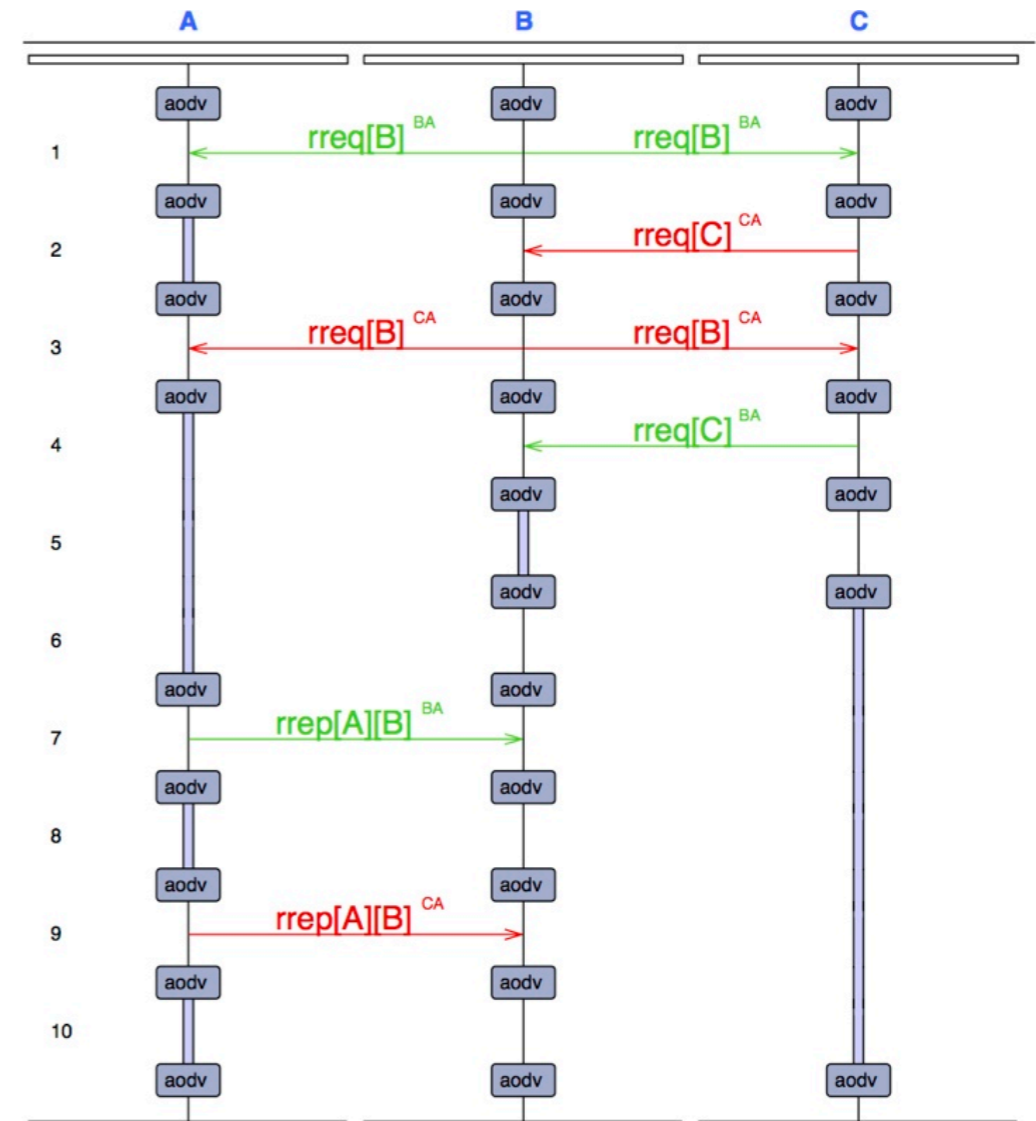
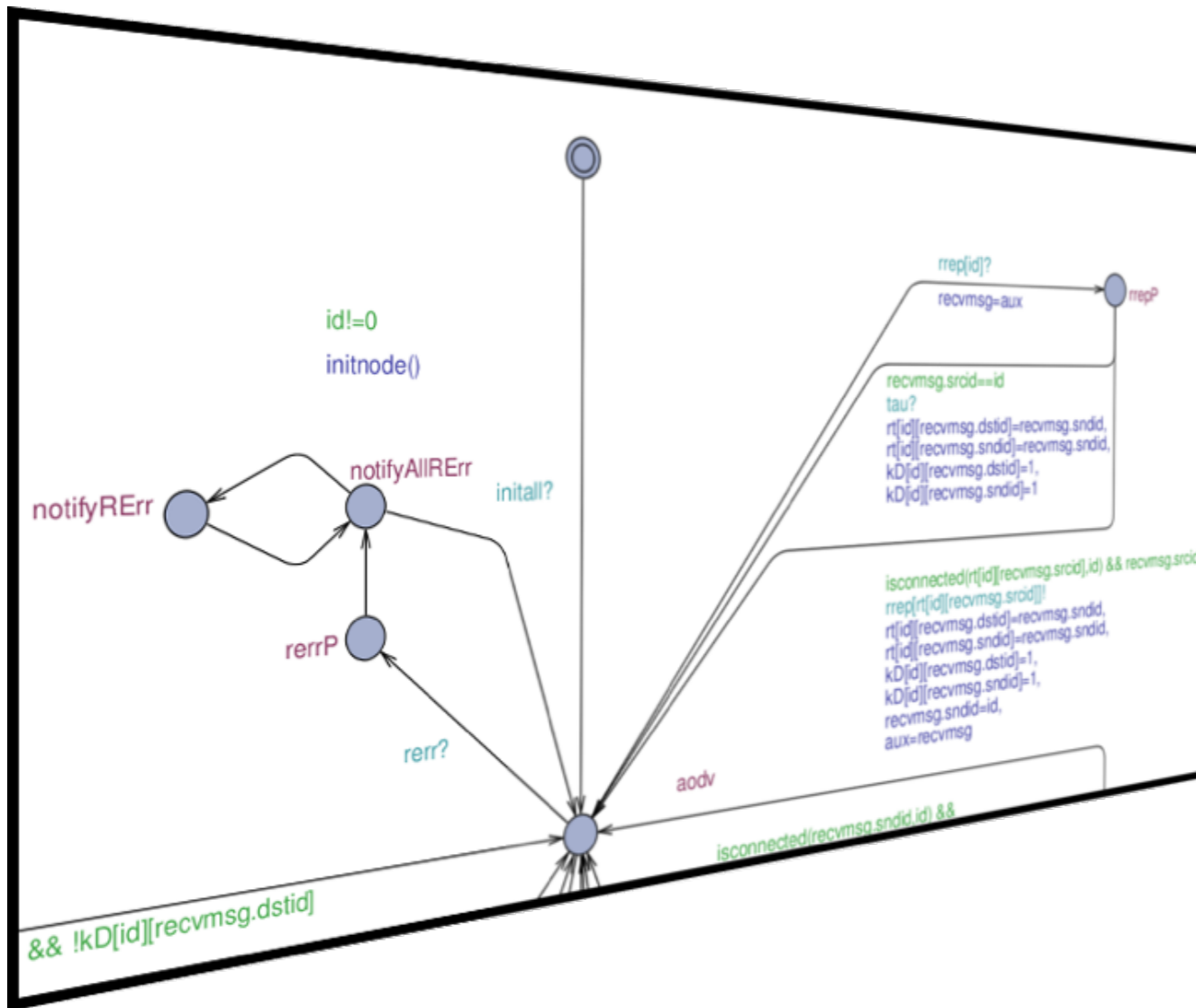
$$ip : P : R \xrightarrow{\text{connect}(ip, ip')} ip : P : R \cup \{ip'\}$$

$$ip : P : R \xrightarrow{\text{disconnect}(ip, ip')} ip : P : R - \{ip'\}$$

- process algebra is blocking (our model is non-blocking)
- process algebra is isomorphic to one without data structure --- a process for every substitution instance
- resulting algebra is in *de Simone* format (by this strong bisimulation is a congruence)
- both parallel operators are associative (follows by a meta result of Cranen, Mousavi, Reniers)

- AODV Routing Protocol
- Achievements
  - full concise specification of AODV (RFC 3561)  
(no time)
  - verified/disproved properties
    - route discovery
    - packet delivery
    - loop freedom
      - first (correct) proof
      - disproved loop freedom for variants of AODV  
(as implemented in at least open source implementation)
  - found several ambiguities, mistakes, shortcomings
  - found solutions for some limitations

# Model Checking



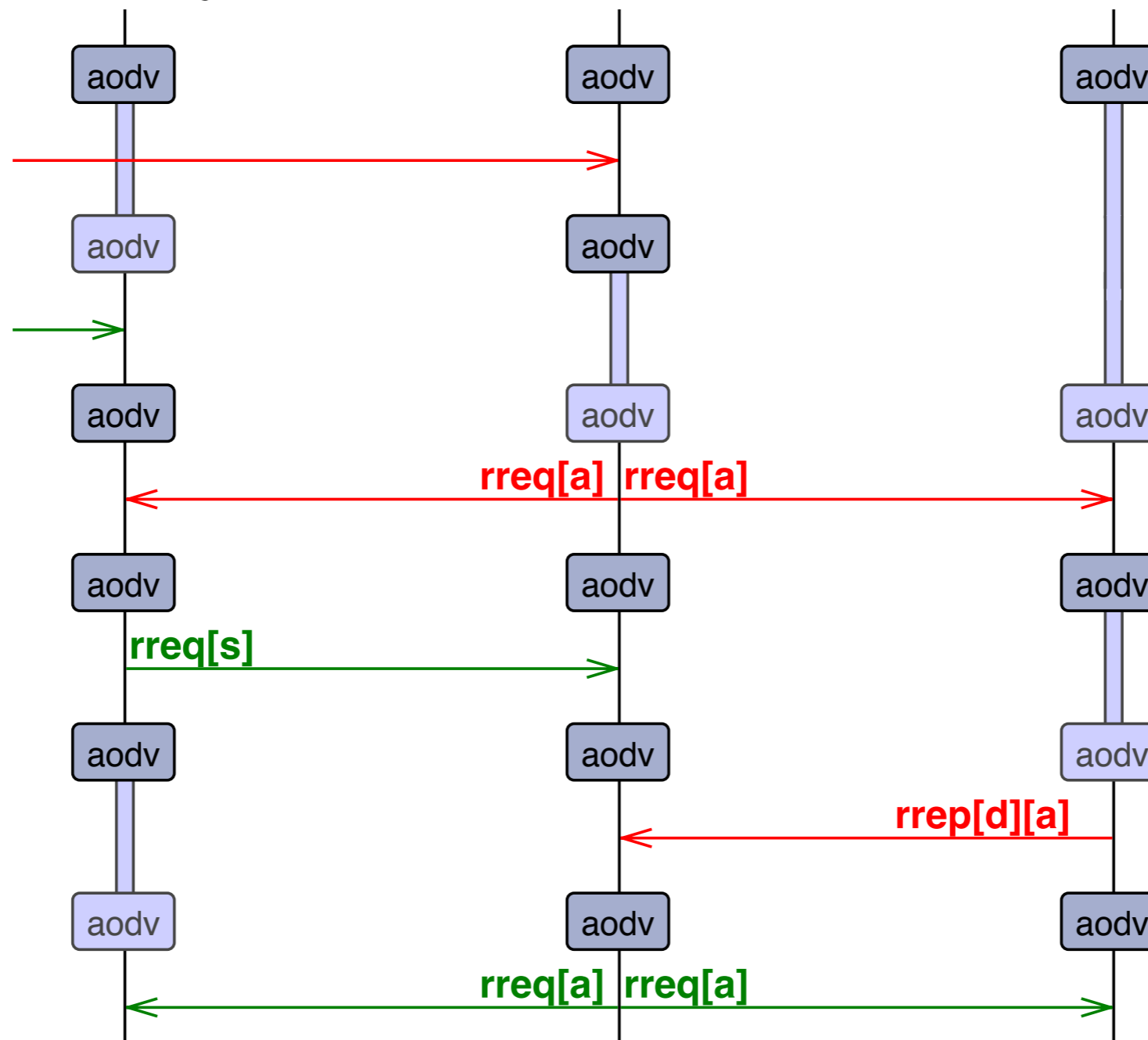


- Model checking routing algorithms
  - executable models
- Complementary to process algebra
  - find bugs and typos in model of process algebra
  - check properties of specification applied to particular topology
  - easy adaption in case of change
  - automatic verification
- Achievements
  - implemented process algebra specification of AODV
  - found/replayed shortcomings

- Well established model checker
- Uses networks of timed automata
- Has been used for protocol verification
  
- Synchronisation mechanisms
  - binary handshake synchronisation (unicast communication)
  - broadcast synchronisation (broadcast communication)
- Common data structures
  - arrays, structs, ...
  - C-like programming language
- Provides mechanisms for time and probability

- Exhaustive search
  - various properties
  - all different topologies up to 5 nodes (one topology change)
  - 2 route discovery processes
  - 17400 scenarios
  - variants of AODV (4 models)

- Route discovery fails in a linear 3-node topology



- exhaustive search  
(potential failure in route discovery)
  - static topology: 47.3%
  - dynamic topology (add link): 42.5%
  - dynamic topology (remove link): 73.7%
- AODV repeats route request
- Other solution: forward route reply

- So far concentrated on AODV
  - well known
  - IETF standard
- Extend formal methods to other protocols
  - OSLR, DYMO, ...
- Add further necessary concepts
  - time
  - probability (links, measurements)
  - define quality of protocols

- Automating process-algebraic proofs
- Advantages
  - verified correctness
  - proof replay for variants
- Isabelle/HOL
  - is it possible within reasonable time?
  - what kind of encoding (deep vs shallow)  
should follow the process algebraic concepts
  - trace-based proofs,  
how to argue/store a history
  - ...



From imagination to **impact**